

Numerical Simulation of Free Convection Heat Transfer of Ferrofluid in an Oval Shaped Closed Loop

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Abstract - Free convective heat transfer capability of kerosene based ferrofluid flowing through an oval shaped two-dimensional closed loop has been investigated numerically. COMSOL Multi Physics, a standard CFD code has been applied for solving the governing equations. A constant magnetic field was applied using permanent magnet and time dependent numerical study has been conducted for laminar fluid flow and heat transfer. The fluid was found to flow under the effect of externally applied magnetic field and spatially varying temperature. Maximum velocity of 4.43 mm/s has been found under the influence of externally applied magnetic field generated by the permanent magnet and flow was observed to be continuous. Temperature and velocity plots have also been plotted reconfirming the candidature of ferrofluid as a coolant for heat transfer applications of mini/micro devices.

Keywords: Ferrofluid, Convective Heat Transfer, Thermo-magnetic Convection, Kelvin body Force

I. INTRODUCTION

Last few decades have witnessed unprecedented growth in the computational power of electronic devices, thereby generating high temperatures during their working. Conventional cooling methods prove to be inadequate in handling high heat flux generated by these devices, thus necessitating the need for smart cooling devices, which can remove heat at such a rate that they can work without breaking down. Ferrofluid driven heat exchangers can provide a potential solution for cooling of such miniaturized devices.

Ferrofluid is colloidal mixture of nano-sized magnetic particle coated with surfactant in a non-magnetic base fluid. The particles are coated with adsorbed surfactant layers so as to keep a stable suspension state and to avoid agglomeration.

Ferrofluid consist of single domain magnetic nanoparticles which are randomly oriented in the carrier fluid. Thus, when such a fluid is subjected to thermal gradient in the presence of an external magnetic field, due to non-equilibrium magnetization in the fluid, the fluid will experience a magnetic body force, called "Kelvin body force" which results in flow of fluid in the direction of higher temperature section [1].

Shakiba and Vahedi [2] studied the effect of non-uniform magnetic field on hydrothermal characteristics of water-

based ferrofluid flowing through a horizontal double-pipe heat exchanger using ANSYS Fluent. Increase in Nusselt number was observed with increase in the intensity of magnetic field.

Aminfar *et al.* [3] numerically examined the hydrothermal behaviour of water-based ferrofluid flowing through a helical channel using the CV technique. Transverse magnetic field was applied to the channel and increase in the flow rate and velocity gradient was observed with augmentation in heat transfer.

Goharkhah *et al.* [4] performed numerical simulations using COMSOL to find efficient arrangement and locations of four electromagnets along the channel for water based ferrofluid flowing through a channel with evenly heated upper and lower Cu parallel plates. The average heat transfer coefficient was found to augment with the frequency of magnetic field and Re.

Wrobel *et al.* [5] studied numerically and experimentally thermo-magnetic convective flow behaviour of paramagnetic fluid in an annular enclosure with a round rod core and a cylindrical outer wall. Results show that magnetizing force affects the heat transfer rate and magnetic convection of paramagnetic fluid can be controlled by a strong magnetic field.

R. Zanella *et al.* [6] numerically studied the transformer cooling using ferrofluid. Vegetable oil seeded with magnetite nanoparticles @ 10% volume fraction was considered. A magnetohydrodynamics code called SFEMaNS was applied on a solenoid system and magnetostatic, Navier-Stokes, and energy equations were solved simultaneously. Numerical results for ferrofluid point out that the magnetoconvection modifies the flow convection pattern and speed and subsequently temperature rise in the coil was reduced by about 9.4% with ferrofluid cooling.

E. Aursand *et al.* [7] proposed a one-dimensional multi-phase flow model for thermomagnetically pumped ferrofluid that includes the effects of heat transfer, friction, gravity, and magnetic forces. The proposed model was also validated against experiments from the literature and was found to give good predictions for the thermomagnetic pumping performance. However, the results also signify

very large sensitivity to uncertainties in heat transfer coefficient predictions.

Tomasz Strek [8] considered the 2D, laminar and incompressible ferrofluid flow between two parallel flat plates. Flow was influenced by magnetic dipole sufficient enough to saturate the ferrofluid using computational fluid dynamics code COMSOL. Heat source in the form of rectangular blocks was placed below the upper wall. It was observed that under the action of Kelvin Body force generated due to interaction between the local magnetic field and the molecular magnetic moments, hotter fluid is being displaced by colder fluid when the magnet is placed near to heat source, thus system as a whole does not require additional energy input except energy from external magnet. Wahid Cheriefet *al.* [9] experimentally analyzed the effect of parameters such as the direction of magnetic field and its level, length of the magnetic source, particle concentration and the mass flow rate on convective heat transfer coefficient and pressure drop for a ferrofluid flowing through a square duct under magnetic field. Augmentation in value of *h* and pressure drop was observed with increase in volume fraction, and low mass flow rates were considered more effective as far as cooling capability is concerned. Magnetic source length has lesser effect on pressure drop; however, heat transfer coefficient is strongly influenced by its length. In addition, best results for convective heat transfer coefficients were achieved when magnetic field was held perpendicular to the heat flux.

The work presented in this paper explores the possibility of ferrofluid to be used as a coolant for heat dissipation of miniaturized devices. Numerical simulation is carried out using COMSOL MultiPhysics 5.0. Governing equations such as momentum and energy equations have been accordingly modified by incorporating term containing magnetic force. Simulations are performed on 2D oval shaped closed loop and results are plotted in the form of velocity and temperature plots.

II. NUMERICAL MODELLING

A. Description of Geometry

A two dimensional model as shown in Fig. 1 is used for simulation study. The model consists of a oval shaped closed loop through which kerosene based ferrofluid would flow, a permanent magnet for applying magnetic field, accumulator acting as a reservoir for the fluid, a heat source and fins for dissipating heat to the surroundings.

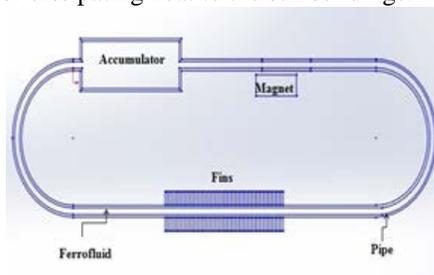


Fig.1 Two dimensional geometrical model

B. Equations governing ferrofluid

Following equations govern the flow of ferrofluid for the problem considered for analysis.

Continuity Equation:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) = 0 \quad (1.1)$$

Momentum Equation:

$$\rho \frac{\partial \mathbf{u}}{\partial t} + \rho \mathbf{u} \cdot \nabla \mathbf{u} = -\nabla p + \nabla \cdot (\mu (\nabla \mathbf{u} + (\nabla \mathbf{u})^T)) - \frac{2}{3} \mu (\nabla \cdot \mathbf{u}) \mathbf{I} + \mathbf{F} \quad (1.2)$$

Energy equation:

$$\rho c_p \left(\frac{\partial T}{\partial t} + \mathbf{u} \cdot \nabla T \right) = k \nabla^2 T + \mu \Phi + \dot{q} \quad (1.3)$$

Magnetic Induction:

$$\mathbf{B} = \mu_0 (\mathbf{H} + \mathbf{M}) \quad (1.4)$$

Kelvin Body Force:

$$\mathbf{F} = (\mathbf{M} \cdot \nabla) \mathbf{B} \quad (1.5)$$

The properties of ferrofluid used for the simulation is presented in Table I.

TABLE I FERROFLUID PROPERTIES

Sr. No	Parameters	Value
1	Viscosity, μ	0.001 N-s/m ²
2	Density, ρ	909.9 kg/m ³
3	Thermal conductivity, <i>k</i>	0.17 W/(m-K)
4	Remanant flux density	1.00 T
5	Relative permeability of magnet	5000.0
6	Surrounding temperature	293.15 K
7	Curie temperature	350 K
8	Magnetic susceptibility	0.3860
9	Relative permeability of fluid	1.3860

C. Simulation

Geometry is created in model builder of COMSOL Multiphysics 5.0 and materials/material properties are assigned to different domains inputting initial values followed by mesh generation. Physics controlled finer mesh with following statistics is created.

TABLE II MESHING STATISTICS

Sr. No.	Property	Value
1	Minimum element quality	0.1173
2	Number of elements	23325
3	Number of vertex elements	352
4	Number of boundary elements	3480

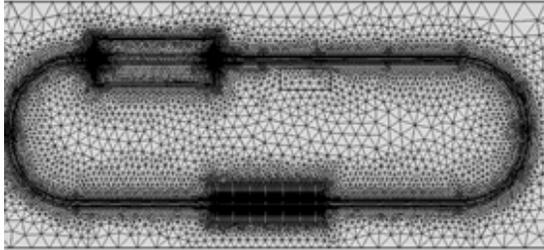


Fig. 2 Meshed model

Since the model involves different physics like magnetic field, heat transfer in solids and laminar flow, thus different physics are combined using conjugate heat transfer option available in COMSOL. Conjugate heat transfer corresponds with the combination of heat transfer in solids and heat transfer in fluids. Magnetic field is considered to be generated by permanent magnets of intensity one Tesla and treated stationary, while heat transfer and laminar flow are treated as time dependent while solving the model.

III. RESULTS AND DISCUSSIONS

Simulation results of temperature generated and velocity produced at different length of time are presented in Fig. 3 and Fig. 4 respectively.

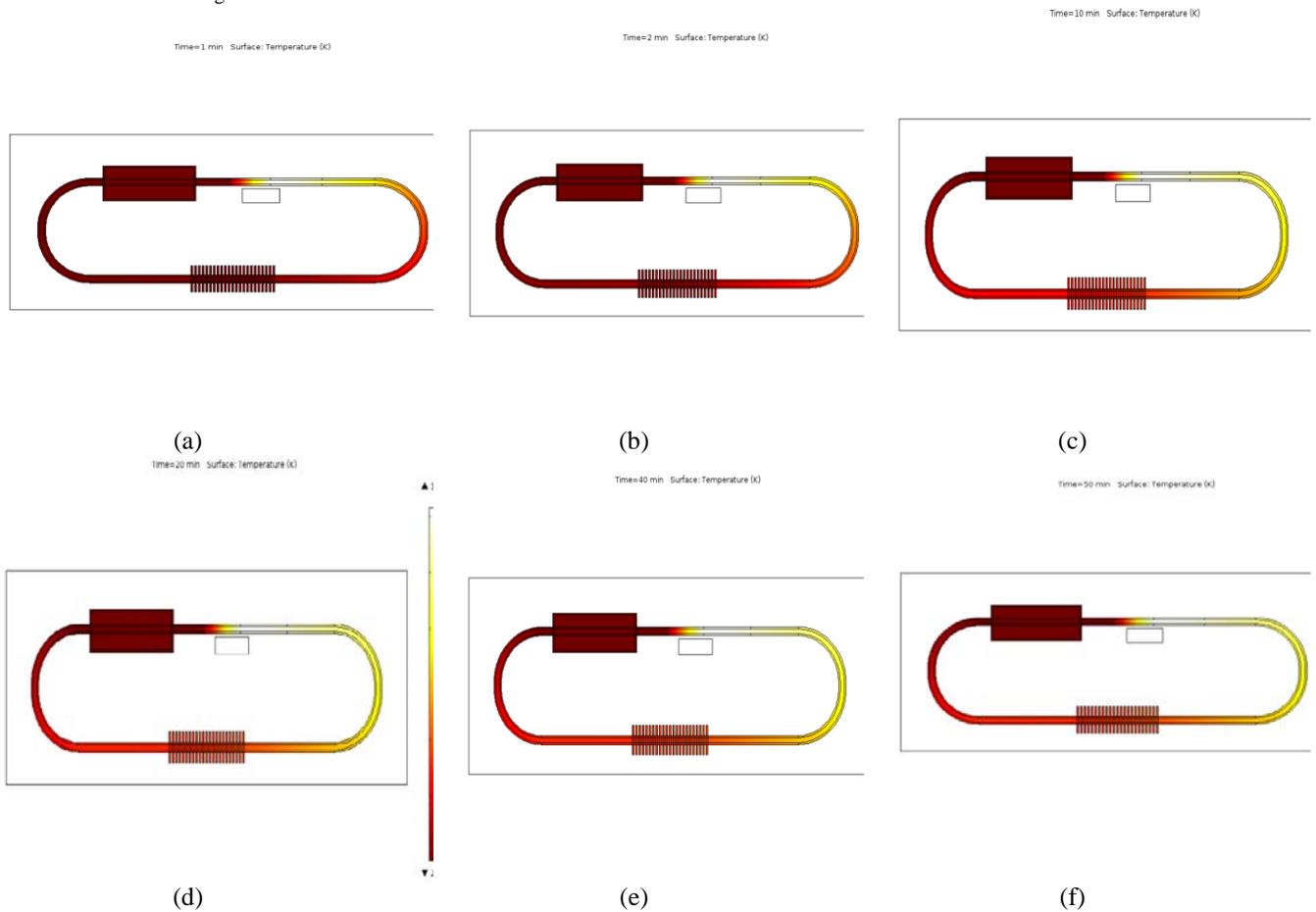


Fig. 3. Fluid Temperature contours (K) generated at different point of time (a) 1min (b) 2 min (c) 10 min (d) 20 min (e) 40 min (f) 50 minutes.

From the time varying temperature distribution diagrams shown in Fig. 3, it can be seen that fluid is heated close to its Curie temperature as it passes through heat source region, and while flowing through the loop, temperature begins to fall as heat loss by convection takes place. But major drop in temperature of the ferrofluid takes place when it reaches/flows in the lower loop and it dissipates its heat through the fin attached on the outer boundary as depicted in the Fig. 3. The fluid becomes cold as it reaches in the accumulator and is ready to absorb heat for the next cycle.

Velocity contours highlight the augmentation in velocity of ferrofluid with time as it flows through the loop. In the beginning, since the temperature difference in the loop is less, lesser velocity is generated as higher temperature difference lead to higher magnetic/Kelvin body force. With the passage of time, temperature profile stabilizes and so is the velocity profile as shown in Fig. 4.

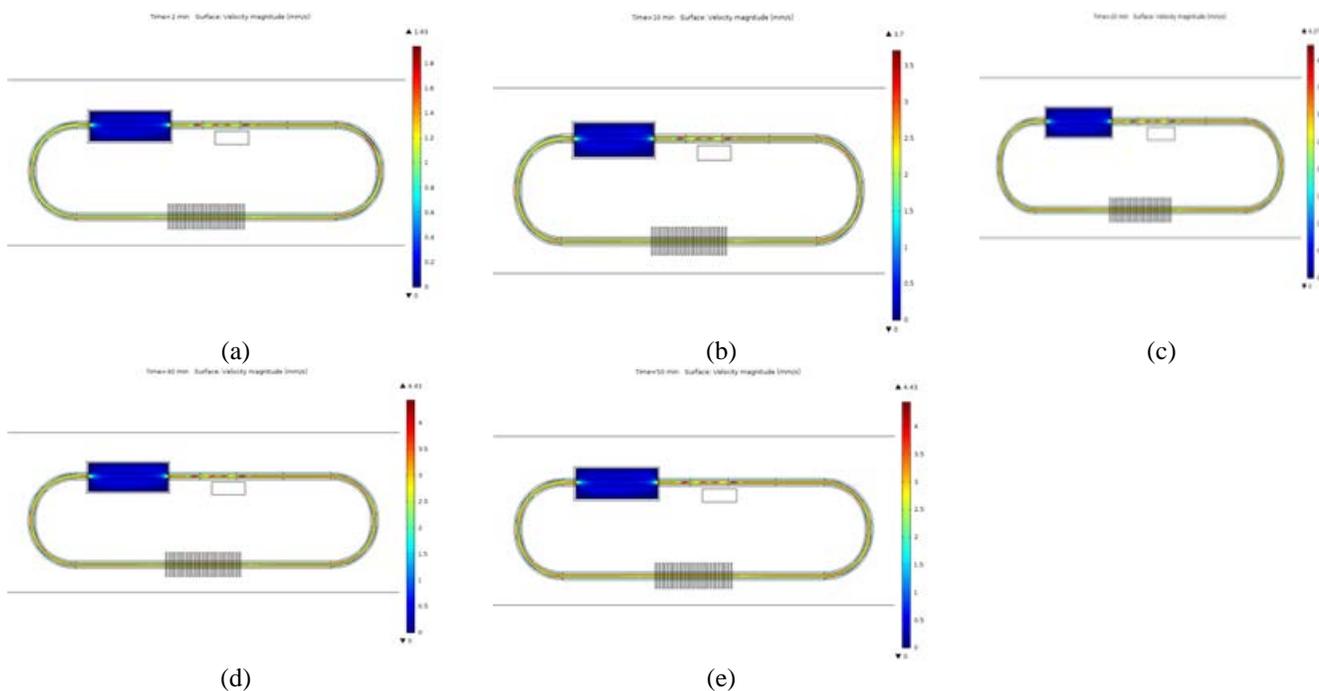


Fig. 4. Fluid Velocity contours (mm/s) generated at different point of time (a) 2min (b) 10 min (c) 20 min (d) 40 min (e) 50 min.

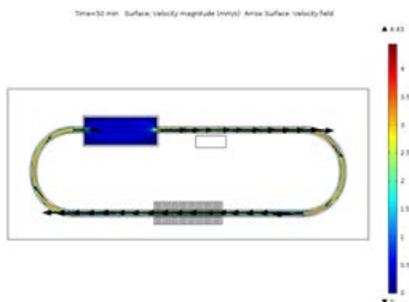


Fig. 5. Velocity vectors representing direction of fluid flow in the loop

IV. CONCLUSION

From the numerical study, following conclusions could be drawn:

1. Temperature plots showing variations of temperature in different parts of loop confirm the removal of heat flux by the ferrofluid, establishing flow of the fluid. Cold fluid is available for extracting heat from the heat source every time after one loop cycle as represented in Fig. 3.
2. Steady state is established after $t = 40$ minutes, as there are minimal or no variations in the temperature profile after that as depicted in Fig 3(e) and Fig. 3(f).
3. Maximum velocity of 4.43 mm/s is found at $t = 40$ minutes i.e. fluid moves under the influence of external magnetic field generated by the permanent magnet of intensity 1 T. The flow has also been found to be continuous in the pipe.
4. Velocity vectors in Fig. 5 shows the direction of fluid flow. Under the influence of Kelvin body force, fluid starts to move in clockwise direction, extracting heat from the heat source and during its passage dissipating

thermal energy to the surroundings through fins attached at the lower end of the closed loop, thus low temperature fluid is always available at the end of every cycle.

The numerical study conducted in this paper signifies the heat transfer capability of ferrofluid as a coolant. The system as a whole is totally passive as it does not require any external device such as pump for circulating the fluid. Moreover, there are no rotating/reciprocating parts, thus operation is noise-free and reliability of the system is excellent. Further research could be carried out to find optimal dimensions of the loop and best combination of different properties that may maximize the thermal performance of the ferrofluid based cooling system.

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